Pearson Edexcel Level 3 GCE

Thursday 14 May 2020

Afternoon

Paper Reference 8FM0/28

Further Mathematics

Advanced Subsidiary Further Mathematics options 28: Decision Mathematics 2 (Part of option K only)

You must have:

Mathematical Formulae and Statistical Tables (Green), calculator, D2 Answer Book (enclosed)

Candidates may use any calculator allowed by Pearson regulations.

Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of the D2 Answer Book with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the D2 Answer Book provided
 - there may be more space than you need.
- You should show sufficient working to make your methods clear.
 Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.
- Do not return the question paper with the D2 Answer Book.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for each question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







1.

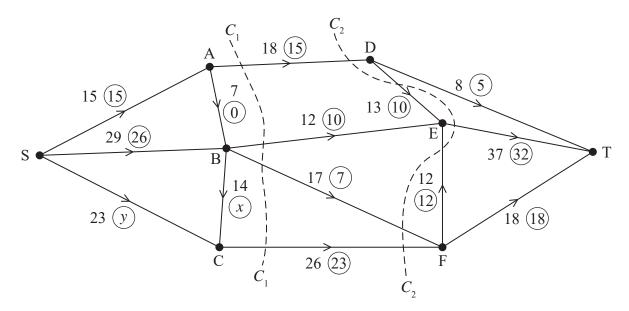


Figure 1

Figure 1 shows a capacitated, directed network of pipes. The number on each arc represents the capacity of the corresponding pipe. The numbers in circles represent a feasible flow from S to T.

(a) (i) Find the value of x.

(b) List the saturated arcs. (1)

Two cuts, C_1 and C_2 , are shown in Figure 1.

(c) Find the capacity of

(i) C_1

(ii)
$$C_2$$
 (2)

(d) Write down a flow-augmenting route, using the arc CF, that increases the flow by two units. (1)

Given that the flow through the network is increased by two units using the route found in (d),

(e) prove that this new flow is maximal.

(Total for Question 1 is 9 marks)

(3)

2. Four workers, A, B, C and D, are each to be assigned to one of four tasks, P, Q, R and S.

Each worker must be assigned to one task, and each task must be done by exactly one worker.

Worker C cannot be assigned to task Q.

The amount, in pounds, that each worker would earn when assigned to each task is shown in the table below.

	P	Q	R	S
A	72	98	59	84
В	67	87	68	86
С	70	- 62		79
D	78	93	64	81

The Hungarian algorithm is to be used to find the maximum total amount that can be earned by the four workers.

(a) Explain how the table should be modified so that the Hungarian algorithm may be applied.

(2)

(b) Modify the table so that the Hungarian algorithm may be applied.

(1)

(c) Reducing rows first, use the Hungarian algorithm to obtain an allocation that maximises the total earnings. You should explain how any initial row and column reductions were made and also how you determined if the table was optimal at each stage.

(6)

(Total for Question 2 is 9 marks)

3. Two teams, A and B, each have three team members. One member of Team A will compete against one member of Team B for 10 rounds of a competition. None of the rounds can end in a draw.

Table 1 shows, for each pairing, the expected number of rounds that the member of Team A will win minus the expected number of rounds that the member of Team B will win. These numbers are the scores awarded to Team A. This competition between Teams A and B is a zero-sum game. Each team must choose one member to play. Each team wants to choose the member who will maximise its score.

		Team B				
		Paul	Qaasim	Rashid		
	Mischa	4	-6	2		
Team A	Noel	0	-2	6		
	Olive	-6	2	0		

Table 1

- (a) (i) Find the number of rounds that Team A expects to win if Team A chooses Mischa and Team B chooses Paul.
 - (ii) Find the number of rounds that Team B expects to win if Team A chooses Noel and Team B chooses Qaasim.

(2)

Table 1 models this zero-sum game.

- (b) (i) Find the play-safe strategies for the game.
 - (ii) Explain how you know that the game is not stable.

(4)

(c) Determine which team member Team B should choose if Team B thinks that Team A will play safe. Give a reason for your answer.

(1)

At the last minute, Rashid is ill and is therefore unavailable for selection by Team B.

(d) Find the best strategy for Team B, defining any variables you use.

(7)

(Total for Question 3 is 14 marks)

4. A sequence $\{u_n\}$, where $n \ge 1$, satisfies the recurrence relation

$$2u_n = u_{n-1} - kn^2$$
 where $4u_2 - u_0 = 27k^2$

and *k* is a non-zero constant.

Show that, as n becomes large, u_n can be approximated by a quadratic function of the form $an^2 + bn + c$ where a, b and c are constants to be determined.

(8)

(Total for Question 4 is 8 marks)

Please check the examination details below before entering your candidate information Centre Number Candidate Number **Pearson Edexcel Level 3 GCE** Thursday 14 May 2020 Paper Reference **8FM0/28** Afternoon **Further Mathematics Advanced Subsidiary Further Mathematics options** 28: Decision Mathematics 2 (Part of option K only) **D2 Answer Book Total Marks** Do not return the question paper with the answer book.

Turn over ▶





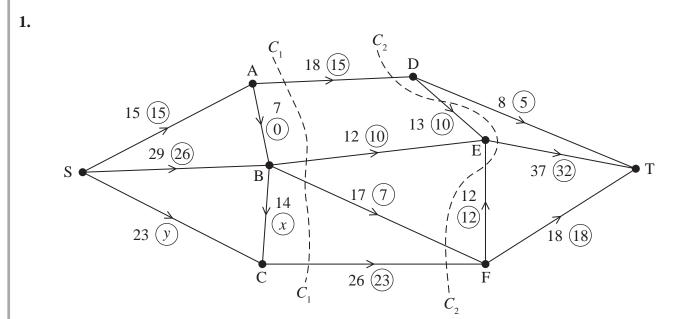


Figure 1

2

Question 1 continued	
(To	tal for Question 1 is 9 marks)



2.

	Р	Q	R	S
A	72	98	59	84
В	67	87	68	86
С	70	_	62	79
D	78	93	64	81

You may not need to use all of these tables.

	P	Q	R	S
A				
В				
С				
D				

	P	Q	R	S
A				
В				
С				
D				

	Р	Q	R	S
A				
В				
С				
D				

6 2				

Question	n 2 conti	nued		
	P	Q	R	S
A				
В				
C	<u> </u>			
D	<u> </u>			
D	<u> </u>			
	P	Q	R	S
A				
В				
С				
D				
	P	Q	R	S
A				
В				
C	<u> </u>			
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	P	Q	R	S
Α	1	<u> </u>	IX	
A				
В				
С				
D				
	n.			
	P	Q	R	S
A				
В				
С				
D				



3.						
			Team B			
_			Paul	Qaasim	Rashid	
		Mischa	4	-6	2	
	Team A	Noel	0	-2	6	
		Olive	-6	2	0	

Table 1

Question 3 continued	



Question 3 continued

Question 3 continued	
(Tota	l for Question 3 is 14 marks)



4.

Question 4 continued	



Question 4 continued
(Total for Question 4 is 8 marks)
TOTAL FOR DECISION MATHEMATICS 2 IS 40 MARKS

